

PIV with LED: Particle Shadow Velocimetry (PSV)

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A particle-shadow-velocimetry (PSV) technique that employs light sources with significantly lower power than lasers is introduced as a variant of particle-image velocimetry (PIV). The PSV technique uses a non-scattering approach that relies on direct in-line illumination by a pulsed source such as a light-emitting diode (LED) onto the camera imaging system. Narrow-depth-of-field optical setups are employed for imaging a two-dimensional plane within a flow volume, and images that resemble a “negative” or “inverse” of the standard PIV scattering mode are produced by casting particle shadows on a bright background. In this technique the amount of light reaching the image plane and the contrast of the seeding particles are significantly increased while requiring significantly lower power than scattering approaches. The limitations of the technique, its velocity ranges, and the setup parameters are discussed.

I. Introduction

PARTICLE-IMAGE VELOCIMETRY - (PIV) is a powerful diagnostic technique that is capable of providing accurate and resolved velocity fields in a variety of applications. High-speed PIV is becoming increasingly important with the emergence of high-speed laser sources and high-speed video cameras.¹ Most PIV techniques require laser light sources that are capable of high-power, short-duration pulses, allowing instantaneous marking of seed particles and capture of their scattered light by an imaging system. Presently lasers are the most expensive component in PIV systems, despite their relatively slow repetition rates in their commercial form. High-speed PIV is even more costly since it also requires expensive high-speed cameras.

In the present paper an alternative approach, particle-shadow velocimetry (PSV), is introduced, which allows low-power illumination sources such as LEDs to be used for PIV in many applications. LEDs are inexpensive and can be pulsed to nanosecond levels and at high-repetition rates;² their use is proposed here for applications to PIV measurements in various fields of view and over various velocity ranges. The PSV technique has further advantages with respect to laser-based PIV because it produces no glare or reflections from surfaces; since LEDs of many monochromatic wavelengths are available, two-color PIV and multicolor PIV is also feasible.

Applications of the technique for large areas through the use of LED clusters to increase short-pulses brightness and strategies for controlling the depth of field for imaging a two-dimensional (2D) plane will be also discussed.

One of the main aims of this research is to develop a technique for use in large-scale, high-speed wind-tunnel applications that can accommodate direct illumination. A schematic of the LED setup for one such application, a transonic-cascade experiment,³ is shown in Fig. 1. The small size of the LED light-source units and their relatively simple wiring also make them attractive and feasible for optical diagnostics inside turbomachines.

II. Particle-Shadow Velocimetry (PSV)

The PSV technique is a variant of PIV that utilizes direct in-line volume illumination and an imaging-optics setup that produces a narrow depth-of-field (DOF) for 2D plane imaging.

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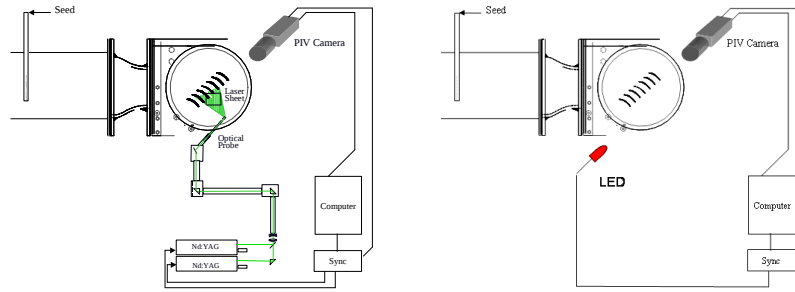


Fig. 1 LED substitutes the laser in transonic-cascade experiment. Narrow DOF imaging substitutes the laser-sheet thickness.

In PSV the setup permits the DOF, the field-of-view (FOV), and the working distance (WD) to be adjusted by introducing spacers or bellows between the camera body and various lenses (Fig. 2). In a simple setup that uses bellows (Fig. 2a), the required extension of the bellows attachment is the product of the reproduction ratio (magnification) and the focal length.

The DOF decreases with the spacing and large aperture and can produce a very thin, focused plane (e.g., sub-millimeter). The addition of more than one lens (Fig. 2b) increases flexibility in the combination of the key parameters (DOF, FOV, WD). Commercially available lenses were used in the present investigation, but custom designs could yield a smaller setup for achieving the desired parameters. For example, since the DOF is proportional to the diameter of the lenses, a larger diameter lens would produce a sharper DOF. In the present study the DOF was on the order of 1-3 mm, and the FOV and the WD could be varied from millimeters to several centimeters. Another mechanism that was considered for controlling key parameters such as the DOF is image post-processing. For example, image filtering allows removal of image data that fall beyond a certain intensity threshold, based on their location from the center of the focal plane. Most PIV techniques utilize such methods. For example, microscopic PIV^{4,5} approaches and miniature PIV with LED⁶ approaches utilize the principle of narrow DOF to image a 2D plane as well as imaging post-processing filtering techniques. Some approaches employ defocusing principles to measure the three-dimensional (3D) velocity field.^{5,7}

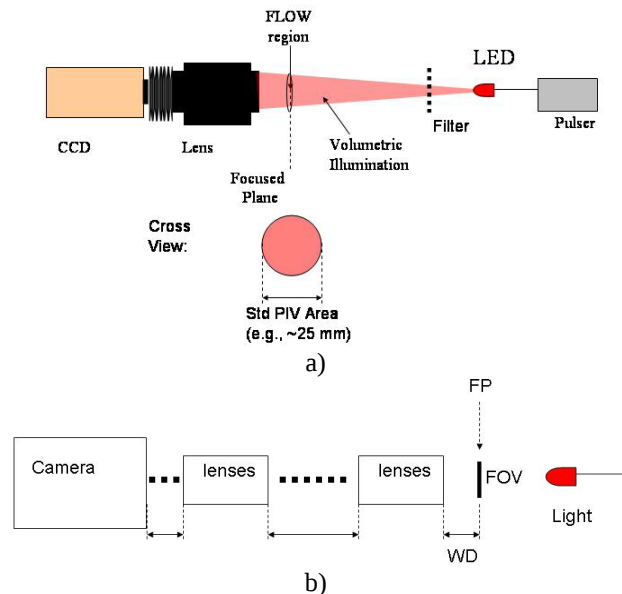


Fig. 2 Examples of PSV-setup schematics with narrow DOF and direct in-line LED volume illumination.

The micro-PIV approaches are often based on fluorescent tagging of particles⁴ or on light scattering through transmitted-light microscopy.⁵ In fluorescence approaches, particles suspended in the flow [e.g., polystyrene latex particles –(PSL)] are tagged with a dye to excite at a certain wavelength (typically chosen to be near the Nd:YAG-

laser wavelengths) and emit at another. In transmitted-light techniques, the light is transmitted from a source on the side of the specimen that is opposite the objective and passed through a condenser to focus it on the specimen for obtaining very high illumination. After the light passes through the specimen, the image of the specimen goes through the objective lens and to the oculars, where the enlarged image is viewed. The most widely used setup for proper specimen illumination and image generation is known as Köhler illumination, and there the micro-PIV applications rely on scattering.

The miniature approach of PIV with LED found in the literature⁶ discusses various setups and results from forward, backward, and side scattering. Because of weak scattering from the LED, the technique is applied only to small areas. In other approaches such as holography, scattering and its interaction with the background light is of major importance when using coherent laser light.⁸⁻¹²

PSV employs a fundamentally different approach that does not rely on principles such as fluorescence, scattering, coherence, Doppler, defocusing, or tagging but on the simpler particle shadow cast on a bright background. This is a consequence of the in-line, zero-degree-deviation direct-illumination setup. Figure 3 is a schematic of the differences between collection-of-scattering and collection-of-extinction (shadow-casting) alignment setups. In the PSV mode the angle between the components is zero. A particle lies between the source and the detector (a camera imaging system in this case) and casts a shadow of a certain area given by the light-extinction characteristics¹³ that can be considerably greater or smaller than the geometrical shadow of the particle. Contrast changes yield particle-shadow-diameter variations and permit the diameter to be adjusted by varying the intensity of the incident light. A brighter light produces a smaller particle shadow and, as a consequence, yields a sharper DOF.

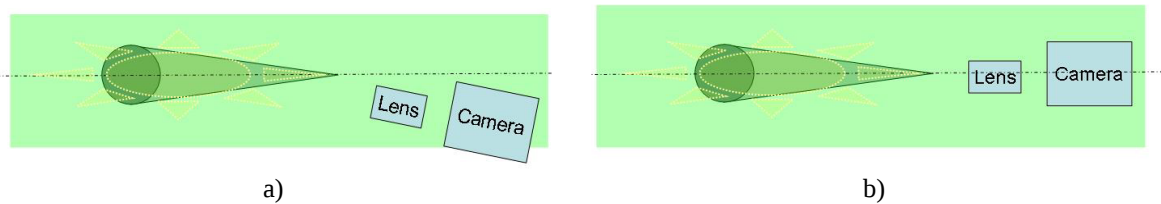


Fig. 3 Schematic of imaging alignment for scattering mode (a) and PSV mode (b), showing spherical particle, its scattering (dashed), and its shadow from background light directed from left to right.

Figure 4 shows image samples comparing the two setups in particle beads on a glass. Having the particles fixed in the glass allows the exposure time to be adjusted and reveals the differences in the images. Both have the same short DOF. The appearance of the images in the PSV approach is that of an “inverse” or “negative” image with respect to that from scattering. For given LED pulse characteristics, the efficiency of the scattering set-up (non-direct illumination) was observed to be very low compared to that of the PSV setup (zero-degree angle of illumination). As with the PIV-with-LED approaches found in the literature,⁶ the capture of scattering images could be accomplished only for very small distances and regions (WD and FOV). In the PSV mode, the LED light is directed straight onto the camera, and shadows of seeding in a bright background result, with a “inverse-PIV” or “negative-PIV” appearance.

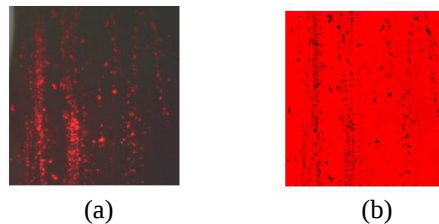


Fig. 4 Side-scattering image (a) and PSV image (b). Particle beads on glass were used.

Although a rigorous study has not yet been performed, some PSV features can be readily explained using particle absorption and scattering-of-light principles¹³ that predict the interaction between light and particles in the present PIV ranges. Of greatest interest here is the light-particle interaction and its effect behind the particle, the region associated with forward scattering or, using a term that shares some terminology with fluid mechanics, the “electromagnetic-wake region.” For example, the following argument clarifies why the region with the highest scattering efficiency--forward--has little to no effect. The particle image recorded on a camera is a result of the

extinction of the (in-line) light caused by absorption and scattering, as opposed to the forward scatter of any light by the particle. The extinction produces a shadow, while forward scatter brightens the particle image. In the basic setup, the only forward scatter that could contribute to the particle image is that of a very small angle, i.e., only the light that would be scattered directly into the recorded image of the particle. All other forward-scattered light would contribute only to an increased background over the entire image. This means that only a small angular fraction of the forward scatter affects the particle contrast. Therefore, the strong forward source light always has a much greater influence than the scattering.

The ratio of extinction to forward scatter depends on the particle size; but in most cases, extinction is ten times larger than forward scatter. This becomes further reduced since the only concern here is forward scatter in a very small angular region. Any scatter outside this region becomes extinction. This consideration likely reduces the ratio from 10 to 1 to more than 1000 to 1. Therefore, it is unlikely that any effects of the forward scatter are recorded.

From a diffraction perspective, it can also be explained that the contribution from diffraction in obscuring the region behind the particle would be negligible, unless the illumination was very strong. There the PSV setup can be thought of as just the inverse of the “slit experiment” for a sufficiently large particle. Therefore, the shadows result; diffraction would keep the light from being completely obscured, but blockage of the source light always dominates. In the Mie-scattering plots, the source intensity is not included; and in any event, it is indeed blocked by the particle (e.g., a geometrical, ideal single ray of light). In practice, all of the source rays that are not scattered by the particle can be detected.

The other crucial component in PSV is the use of short DOF to image (or cast) the focused shadows. The length of the shadow is a function of the intensity of the illumination, based on the previous arguments. Micro-PIV studies⁴ have shown that in a volumetric illumination, all particles in the volume contribute to scattering. Extension to the PSV technique, where scattering is “overshadowed,” yields a volumetric-particle shadow field that has similar results in the focal plane; that is, shadows are observed only when they are in focus with the maximum in the focal plane and become invisible (in the form of fainting background noise) when out of focus (Fig. 5). The rate of defocusing can also be assumed to be proportional to the diffraction pattern of the particles (assuming that they are point sources imaged through a circular aperture or lens), the pattern having a maximum intensity (corresponding to the Airy function for Fraunhofer diffraction) at the focal plane of the lens (Fig. 6) and decreasing very rapidly. Typically the DOF is arbitrarily defined as a specified fraction of that maximum. The overall signal-to-noise ratio can be improved through filtering, brightness, and seeding density. Therefore, for planar PSV measurements, the out-of-focus contribution can be minimized in the final contribution to the velocity correlation. Alignment is very critical also since aberrations (e.g., spherical) can occur if the components in the optical path are misaligned.

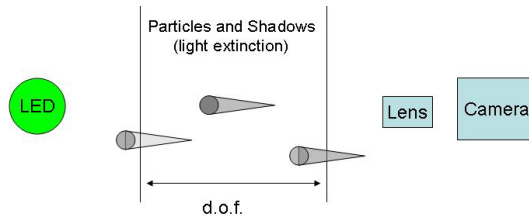


Fig. 5 Contribution of particle shadows to image is restricted to focal plane, with greater contribution from those at the center.

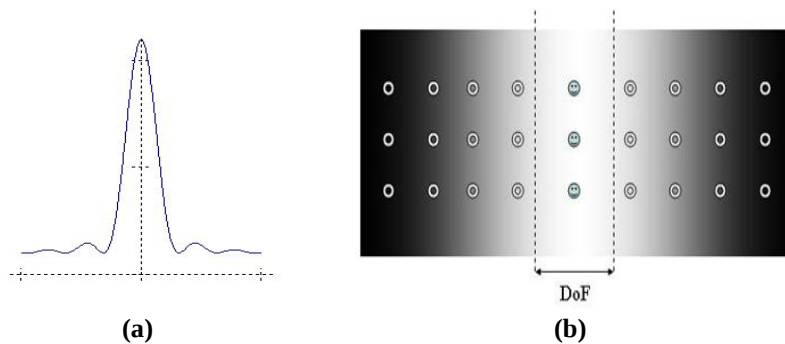


Fig. 6 With sharp DOF, all particles in illuminated volume scatter light and produce shadows, but diffraction pattern (a) has maximum intensity (Airy function) at focal plane of lenses. DOF is defined as specified fraction of that maximum. This effectively results in only 2D slice of illuminated volume being imaged (b).

In PIV, velocity is found by calculating the particle ensemble displacements between two instantaneous time snap-shots, which is generally accomplished through correlation techniques such as using FFT on the image signal. The signal information is generated from changes in intensities; therefore, the same technique can be used for PSV since it is based on information from particle ensembles, although the intensity information is inverted to that from PIV. A subtle difference is that in PIV the particles intensities have a shape such as Gaussian whereas in PSV this shape has not been determined yet and depends on the aforementioned light-particle interaction characteristics. Although this appears to have a negligible effect (e.g., in the correlation peak finding) the method has been calibrated for accuracy as will be explained in the following section. Moreover, since the interest is in the shift or displacement between two signals rather than the signal characteristics themselves, techniques such correlation are applicable to that effect. The PSV image with particles having the lowest intensity compared to the maximum intensity of the background can be readily inverted and generate a PIV-like signal if desired, as will be shown in the following section.

III. Results

In this section some results pertaining to the PSV technique are presented to proof the concept validity and feasibility. First, some samples of LED pulses are displayed, together with some applications showing their capabilities; next, images from a variety of particles and conditions are compared; then, some results from filtering techniques are presented; and finally, some results of flow tests with jets in water and air for several particle sizes and shapes are presented.

The fact that the LED can be pulsed at any rate made it very attractive for velocimetry. This capability is not shared by other sources like lasers or Nanopulsers² which generally have lower and fixed repetition rates (although shorter pulses at present). Pulses from LEDs that were used ranged from tenths of nanoseconds to microseconds. The choice of pulse depends on the velocity of the flow and the magnification, and the pulse must be sufficiently short to freeze the motion while providing sufficient illumination. The red LED is preferred since the CCD camera has its higher spectral sensitivity in the upper-red region. However, an available blue cluster (ISSI) was used to obtain most of the present results because it provided brighter shorter pulses. A red LED cluster will be tested in the future in attempts to gain more efficiency and shorter pulses that would be a requirement in many transonic and higher speed applications. A single LED can be also used if the velocity ranges and other parameters (WD, FOV) are appropriate.

Some sample pulses are shown in Fig. 7. It can be observed that short pulses can be obtained in the range of tenths of nanoseconds (a), even though they are shaper in the microsecond range (b). A train of pulses is also possible, as shown for the case of 100-nsec pulses (c, d). The vertical axis is in arbitrary units (A.U.) since it is the measured voltage from a photodiode. The actual optical energy was not measured. However, the amplitudes shown (except for “d”) can be compared since measurements were made under the same conditions. The photodiode has a rise time of tenths of nanoseconds, which should be taken into account when analyzing the pulses. Because of heat limitations, the LEDs have a limited duty cycle; therefore, unlimited pulses at very high repetition rates would require special designs.

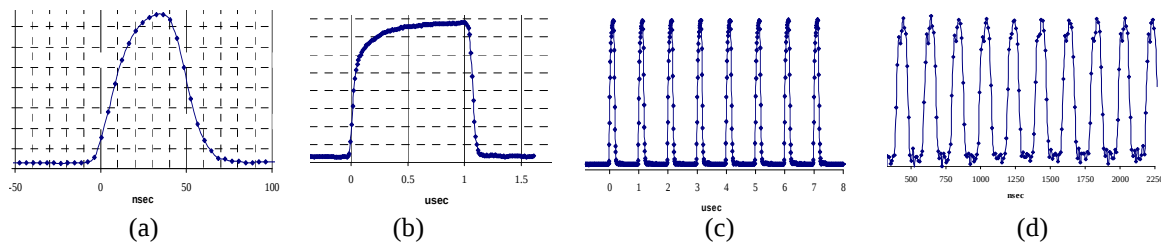


Fig. 7 LED pulse-shape samples: 40 nsec (a), 1 μsec (b), and train of pulses 100 nsec wide at repetition rate of 1 μsec (c) and 200 nsec (d). Y-axis is A.U. (voltage from photodiode).

The camera used in the present experiments was a standard cross-correlation PIV camera (ES1) with 1k x 1k pixels at a 15-Hz repetition rate. Other cameras with higher sensitivity and higher repetition rate were not tested but could be used to achieve better results. On the other hand, relatively inexpensive commercial cameras with detachable lenses have high resolution (although slow repetition rate) and could also be used in the auto-correlation or the two-color-PIV mode.^{14,15} If these cameras were coupled with a single LED, a very inexpensive PIV system could be achieved that would still useful for many experiments and yield high-resolution, accurate results.

The effect of exposure time is readily demonstrated in an air flow seeded with 10 micron ($10\text{-}\mu$) cornstarch particles (Fig. 8). With short pulses the particle shadows appear to be instantaneously frozen (a), but with longer exposures their traces appear (b). In a region of the flow with gradients, both particles and traces are observed (c). Traces could be used to generate velocity vectors, as in particle-streaking velocimetry, although the possibility of out-of-plane motion can produce uncertainties. For the auto-correlation and multiple-exposure mode, a train of pulses can be used; here they are shown in the double-exposure (auto-correlation) mode and multiple-exposure mode in a single frame (Fig. 9) for a slow flow with bubbles. The frames are also shown with image inversion to allow comparison with the standard PIV view (c, d). It can be noted how larger bubbles cast a bright spot in their center because of their lens effect, which focuses the light into a spot.

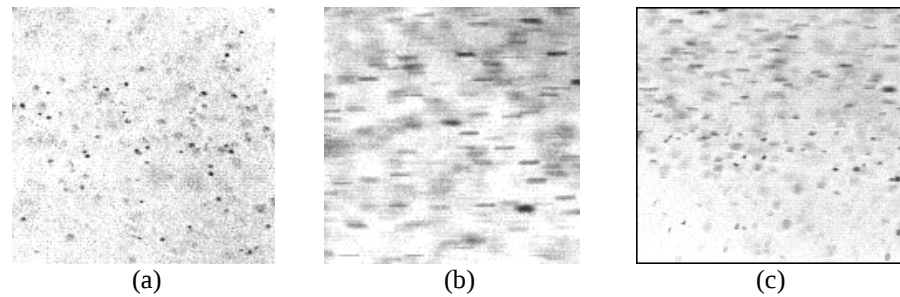


Fig. 8 Exposure time effect. Air jet seeded with cornstarch ($10\text{-}\mu$ diam) particles; details showing point (a), traces (b), and gradient (c) when LED pulse is $1\text{ }\mu\text{sec}$ exposure (a) and $5\text{-}\mu\text{sec}$ (b, c). Images show detailed regions with FOV of few millimeters from a larger image.

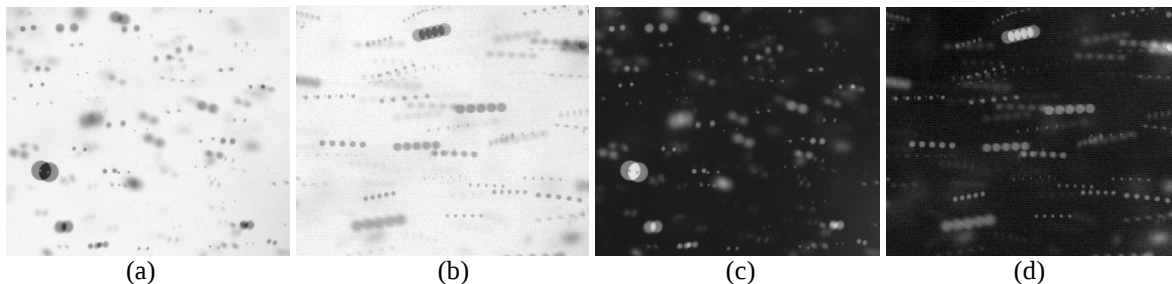


Fig. 9 Auto-correlation or single-frame double-exposed mode (a, c) and multiple-exposure mode (b, d). Particles are bubbles from jet in water. Exposure time was $4\text{ }\mu\text{sec}$ and DT 1 msec . Their inverted images are also shown (c, d) for comparison with standard PIV images. Images are detailed regions with FOV of various millimeters from a larger image.

The effect of coherence was also explored. Figure 10 compares a detail of bubble shadows from LED and laser light. The LED was tested initially with diverging, focused, and collimated illumination and yielded similar results. Laser light was collimated in a larger diameter beam and attenuated prior to directing it to the camera, in a similar manner as when performing digital in-line holography.^{9,10} Both cast particle shadows. LED images could be obtained with pulses on the order of hundreds of nanoseconds.

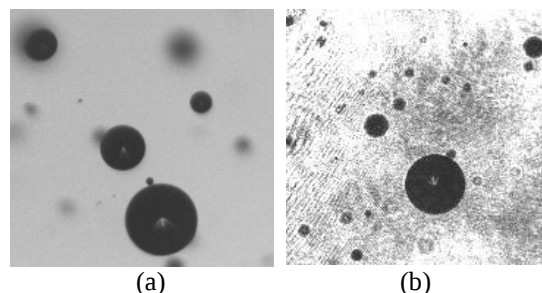


Fig. 10 Comparison of LED light versus coherent laser light in PSV mode. Bubble shadows from LED (a) vs laser coherent light (b); LED $4\text{ }\mu\text{sec}$.

It is obvious that PSV images contain a variety of background-noise textures due mostly to out-of-focus data. Their contribution to the correlation function can be reduced significantly by the optical characteristics of the technique; since these textures contribute to noise, they should be removed. During the experiment this can be done by increasing the illumination; but it can also be accomplished during post-processing by applying filtering techniques that effectively reduce that noise level and produce a sharper image, effectively reducing the 2D plane thickness. One example is shown in Fig. 11 where a threshold intensity filter was applied. Other filters available are based on analysis of the spectral content of the image and removal of the frequencies associated with noise. The image is orange due to the combination of the two greyscale frames in a two color mode (first frame colored red and second colored green) for presentation purposes. The inverted image is also added [Fig. 11(c)] for comparison with the laser-sheet image [Fig. 11(d)] obtained from the same flow. In an effort to perform further calibration of the technique, the flows were used to calculate velocity fields from LED and from laser sheets, and paired-statistical analyses showed negligible differences.

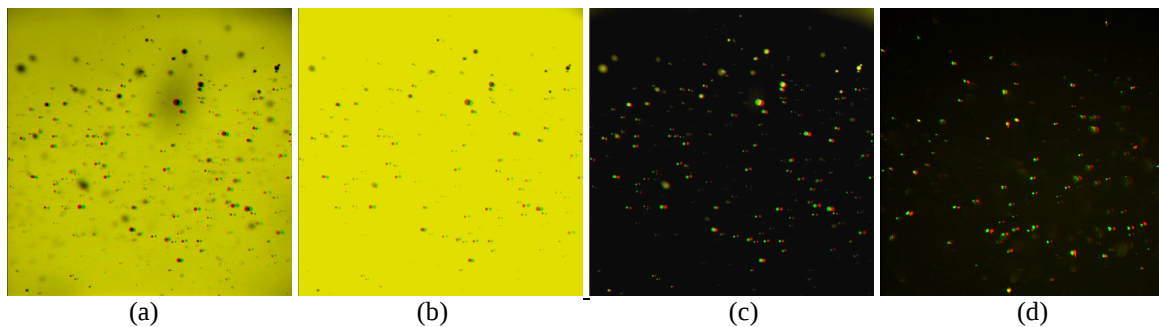


Fig. 11 Image post-processing to reduce out-of-focus and other background noise. Bubbly-jet images are shown for PSV original (a) vs filtered (b). Filtered image is also shown inverted (c) and compared with laser-sheet PIV image (d) of the same flow.

The particle size, its image-shadow size, and their relation to the illumination intensity were explored experimentally to assess the feasibility of the technique in various flow media. Figure 12 shows samples of bubbles imaged with 500-nsec pulses (a), submicron-sized PSL particles in water (b), and cornstarch (10- μ diam) in air with two exposure times (c, d).

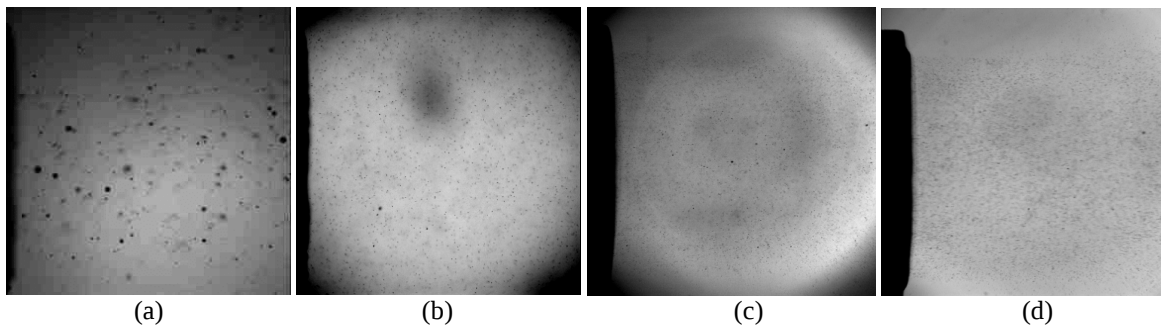


Fig. 12 Media, particle size and shape, and exposure-time effect: a) water jet (bubbles), 500-nsec exposure; b) water jet (PSL, 1- μ diam), 4 μ sec exposure; c) air jet (Cornstarch 10- μ diam) 1 μ sec exposure; d) same as (c) with 5 μ sec exposure FOV~10 mm.

Experiments were also conducted to assess experimentally the effect of the seeding density, and it was found that high-density seeding was also feasible since it did not have significant effect on the sharp DOF plane and velocity field. The cloud of seed remains invisible outside the DOF plane, and correlation could be readily obtained. Figure 13 shows two images (each two-color combined) for comparing medium seeding and heavy seeding. Both provided excellent correlation maps [sample shown in Fig. 13 (c)].

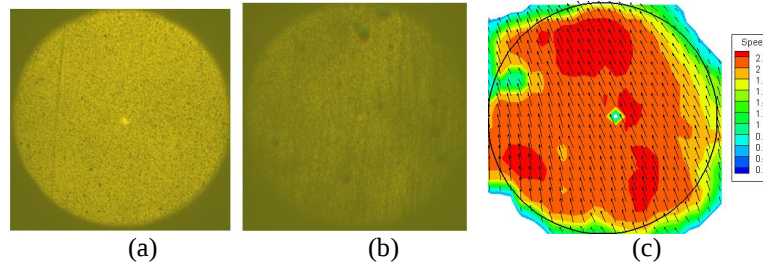


Fig. 13 Effect of seeding density: Medium (a) and heavy (b) and a velocity field (c). Exposures=200 μ sec, DT=5 μ sec, FOV $\sim$ 25 mm.

Finally, some examples of velocity fields obtained with the PSV technique are presented. Figure 14 shows an example of double exposure from free flow using sub-micron smoke particles (mixture of glycerin and ionized water). A single LED (blue) in PSV “in-line” mode with two exposures of 100 μ sec and 5 μ sec apart was used (FOV is 3 mm). Figure 15 shows the PSV image and its derived velocity field from a jet in water using PSL seed (FOV is 10 mm), and Fig. 16 shows an air jet seeded with 10- μ cornstarch particles (FOV is 10 mm).

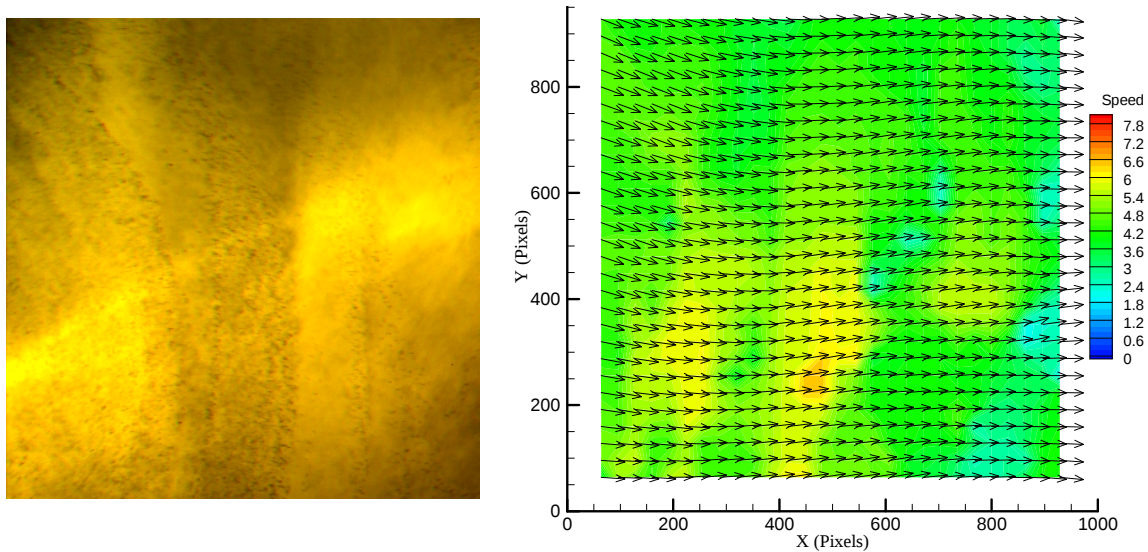


Fig. 14 PSV with LED. Example of air flow with smoke particles (0.5- μ diam); FOV = 3 mm.

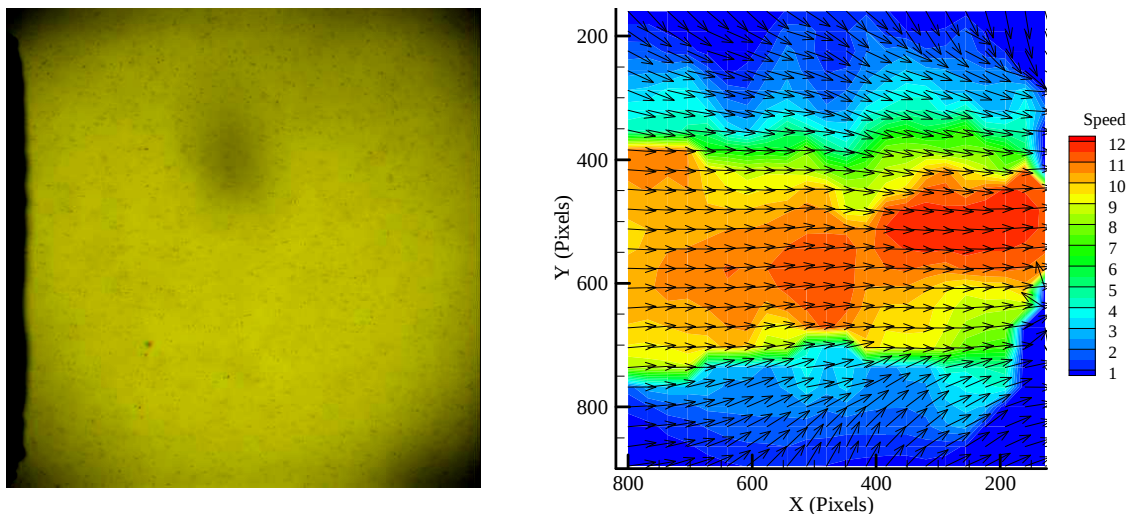


Fig. 15 PSV with LED. Example of water-jet flow with PSL particles; FOV=10mm.

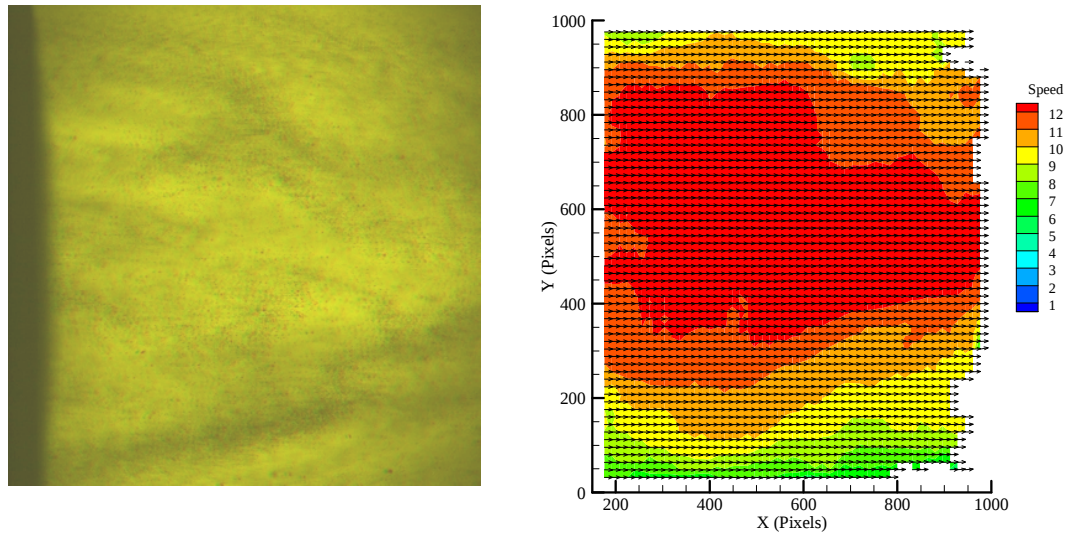


Fig. 16 PSV with LED. Example of air jet flow with cornstarch particles (10-micron); FOV=10mm.

The technique can also be used for flow visualization. Figure 17 is an example of flow visualization using PSV with LED in PSV mode, showing three instants of a drop of water heavily seeded with PSL particles into water.

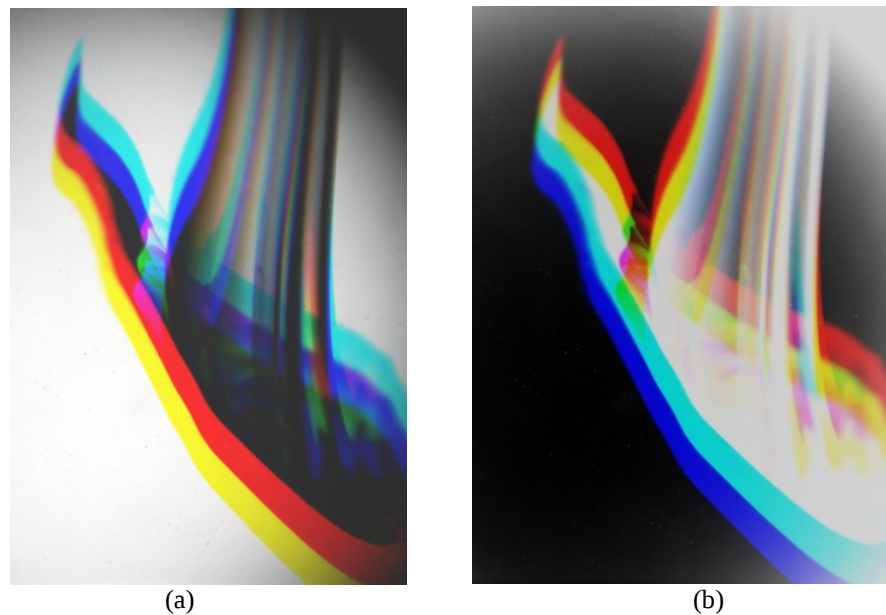


Fig. 17 PSL drop into water; three instants (colored). PSV original (a) and inverted (b).

Another attractive result of the technique is that, in addition to the significant reduction in cost by using LEDs rather than lasers, the camera need not be a costly PIV cross-correlation camera; a commercial less expensive camera in auto-correlation mode or in the two-color mode can be used.^{14,15} In the color-camera approach, the chip has red, green, and blue filters on the pixels (RGB). Each color plane RGB reacts only to that color, in principle. The exception is cross-talk between channels. This is solved in a manner similar to that used in a normal multiple-color PIV case, namely, by subtracting a small portion of the offending color plane from the color plane of interest. For example, if the red bleeds into the green by 10%, then this would be handled by subtracting 10% of the red image from the green. This is effective because the amplitude of the correlation peak is weighted by the number of pairs in the interrogation area, the size of the particle pairs, and the intensity of the pairs. By subtracting a bled component (red), the normal component (green) is effectively enhanced. This was tested with a commercial color camera, and a small bled between the blue and green components based on a RGB LED lamp (ISSI), was cleaned by

subtracting a small portion of the green from the blue. Two-color PSV-with-LED results and other applications such as particle sizing will be presented in a future paper.

IV. Conclusions

A PSV technique was introduced as a variant of PIV. This technique allows light sources with significantly lower power than lasers to be used. The technique employs a non-scattering approach that relies on direct in-line illumination by a pulsed source such as a LED onto the camera imaging system. The technique then uses narrow depth-of-field optical setups for imaging a two-dimensional plane within a flow volume and produces images that resemble a “negative” or “inverse” of the PIV mode by casting particle shadows on a bright background. In this technique the amount of light reaching the image plane and the contrast of the seeding particles are significantly increased while requiring significantly lower power than scattering approaches. Limitations and advantages of the technique, the velocity ranges covered, and other parameter ranges were discussed.

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References

- ¹Boxx, I. G., Idicheria, C. A., and Clemens, N. T., “Kilohertz PIV/PLMS of Low-Gravity Turbulent Flames in a Drop Tower,” 12th International Symposium on Application of Laser Techniques to Fluid Mechanics, Lisbon, Portugal, 2004.
- ²Estevadeordal, J., Gogineni, S., Kimmel, R., and Hayes, J., “Schlieren Imaging for Hypersonic Plasmas,” AIAA Reno, NV, Jan 5-8, 2004
- ³Estevadeordal, J., Car, D., Gorrell, S., and Puterbaugh, S., “DPIV with LED Illumination: Application to Turbomachinery and Flow Control,” Presented at the 29th Annual AIAA Dayton-Cincinnati Aerospace Science Symposium, 9 March 2004, Dayton, OH; also in *Application of Advanced Laser Diagnostics to High Impact Technologies*, Quarterly Report 2829-3 on Contract F33615-03-D-2329 (Innovative Scientific Solutions, Inc., Dayton, OH, 2004).
- ⁴Meinhart, C. D., Wereley, S. T., and Gray, M. H. B., “Volume Illumination for Two-Dimensional Particle Image Velocimetry,” *Meas. Sci. tech.* **11**, 809, 2000.
- ⁵Ovryn, B., “Three-Dimensional Forward Scattering Particle Image Velocimetry Applied to a Microscopic Field-of-View,” *Exp. Fluids [Suppl.]* **S175-S184**, 2000.
- ⁶Chetelat, O. and Kim, K. C., “Miniature Particle Image Velocimetry System with LED In-Line illumination,” *Meas. Sci. tech.* **13**, 1006, 2002.
- ⁷Pereira, F., Gharib, M., Dabiri, D., and Modarress, D., “Defocusing Digital Particle Image Velocimetry: a 3-Component 3-Dimensional DPIV Measurement Technique. Application to Bubbly Flows,” *Exp. Fluids [Suppl.]* **S78-S84**, 2000.
- ⁸Barnhart, D. H., Adrian, R. J. and Pappen, G. C. 1994 “Phase conjugate holographic system for high resolution particle image velocimetry” *Appl. Opt.* **33** 7159–70, 1994.
- ⁹Estevadeordal, J., Copenhaver, W., Car, D., Koch, P., Ng, W., Guillot, S., and Carter, C., “Macro- and Milli-DPIV Studies of a Boundary-Layer-Based Flow-Control System for a Transonic Cascade,” 11th International Symposium on Application of Laser Techniques to Fluid Mechanics, Lisbon, Portugal, 2002.
- ¹⁰Xu, W., Jericho, M. H., Meinertzhagen, I. A., and Kreuzer, H. J., “Digital In-Line Holography of Microspheres,” *Appl. Opt.* **41**(s5), 5367-5375, 2002.
- ¹¹Meng, H., and Hussain, F., “In-line Recording and Off-Axis Viewing technique for Holographic Particle Velocimetry,” *Appl. Opt.*, **34**, 1827-40, 1995.
- ¹²Sheng, J., Malkiel, E., and Katz, J., “One Beam Two View Holographic Particle Image Velocimetry System,” Proc. 4th Int. Symp. on Particle Image Velocimetry, Gottingen, Germany, Paper 1022, 2001.
- ¹³Bohren, C. F., and Huffman, D. R., *Absorption and Scattering of Light by Small Particles*, John Wiley and Sons. 1983.
- ¹⁴Post, M. E., Trump, D. D., Goss, L. P., and Hancock, R. D., “Two-Color Particle Image Velocimetry Using a Single Argon-Ion Laser,” *Exp. Fluids* **16**, s. 263-272, 1994.
- ¹⁵Gogineni, S., Goss, L., Rivir, R., and Pestian, D., “Two-Color Digital PIV Employing a Single CCD Camera,” *Exp. Fluids*, **25**(4), 320-328, 1998.